

CARBON-13 CHEMICAL SHIFTS AND ELECTRONIC STRUCTURE OF METHYLENE GROUPS IN HYDROCARBONS*

Introduction

Direct methods that allow to study the geometric and electronic structure of the carbon skeleton of hydrocarbons are not numerous. There are no chemical methods of general applicability for the determination and investigation of even such simple functional groups as methyl, methylene or methine carbons in saturated chains and indirect methods have to be used to study these. In addition to optical, mainly refractometric, methods molecular spectroscopy has been applied to the study of hydrocarbon structure. Infrared and ultraviolet spectra have been widely used, but the utility of the latter is confined mainly to π -electron systems in aromatic or unsaturated compounds while the former depend first of all on carbon-hydrogen, not carbon-carbon bonds. It is practically impossible to make sound conclusions about the electronic structure of saturated chains or cycles from optical spectra.

Proton magnetic resonance spectra have also been used to study the structure of hydrocarbons. Several useful relationships have been found, the spectral patterns of the methyl groups are characteristic of the chain branching and both methyl

and methylene patterns are indicative of methylene chain length¹, while the chemical shifts of unsaturated and α -protons are susceptible to steric isomerism^{2,3}. But the shift difference is erratic and small, 0.04 to 0.10 ppm only and most specific difference in spin-spin couplings for *cis* and *trans* isomers cannot usually be measured from the very complicated spectra. Proton spectra have proved to be especially useful in the analysis of strained polycyclic hydrocarbons⁴, particularly together with double resonance methods⁵. In this particular case the spin-spin coupling constants are sometimes more useful than chemical shifts that are often influenced by magnetic interactions in an unpredictable manner⁶. The hydrocarbons always contain large strongly coupled systems and the proton spectra of these molecules are very complicated. It is just impossible at present to measure the chemical shifts of all protons in more complicated molecules than pentenes. If double resonance can in this case accomplish partial simplification.

The carbon-13 spectra offer in this respect several important advantages. While the total range of chemical shifts of methylene protons in unsaturated hydrocarbons does not exceed 4 ppm, well over 99 % of all shifts crowded into a small 2 ppm range, the total span of carbon-13 chemical shifts is 80 ppm for saturated methylene groups in hydrocarbons. This amounts to 1/3 of the total

* The lecture was delivered at the Meeting on Chemistry 1967 in Helsinki.

carbon-13 chemical shifts. The low energy of carbon-13 nuclei (1.08 per cent of the rest mass) makes it difficult to back as it makes the registration of the signal difficult, but on the other hand it brings important simplification of carbon-13 spectra. The main reason for this is that in no line splittings as a result of coupling between carbon atoms. If one decouples with a strong coherent field acting on the hydrogen spins, the carbon-13 spectrum consists of single lines for each carbon atom.^{2,3,9,10,11} For large molecules, at present with the use of the empirical constitutive method, the carbon-13 spectra of the saturated hydrocarbons and carboxylic acids can be viewed as a consequence of the electronic structure of these molecules. These shifts can be calculated using useful analytical relationships between the carbon-13 chemical shifts and molecular structure.¹²

Theory with a basis set consisting of a 1s Slater orbital on each hydrogen atom in the molecule, and 2s and 2p Slater orbitals on each carbon atom. All neighbour and non-neighbour interactions are included (non-zero differential overlap) and the complete secular determinant is treated. A somewhat different approach has been used by Whitehead. His self-consistent group orbital and bond electronegativity (SGOBE) method^{23,24} and the extended Hückel theory (EHT) have both been used for charge calculations and gross atomic charge Q_k has been found to correlate successfully with the carbon chemical shifts²³, thereby providing an important link between theoretical calculations and experiment.

The total screening of a nucleus can be divided into a diamagnetic and a paramagnetic contribution from local currents associated with the given atom A, contributions from local currents on other atoms B and effects of molecular ring currents that cannot be localized^{25,26}. The magnetic field at nucleus A is

$$H_A = H_0 (1 - \sigma^A), \quad (1)$$

where σ^A is the total shielding constant of a particular nucleus.

$$\sigma^A = \sigma_p^{AA} + \sigma_d^{AA} + \sum_{B \neq A} \sigma^{AB} + \sigma^{A, ring} \quad (2)$$

The local paramagnetic term is given by

$$\sigma_p^{AA} = -\frac{e^2 \hbar^2}{2 m^2 c^2 \Delta E} \left\langle r^{-3} \right\rangle_{2p} \sum_B Q_{AB}, \quad (3)$$

where ΔE is the mean $\sigma \leftrightarrow \pi$ excitation energy, usually 5 to 10 eV, $\left\langle r^{-3} \right\rangle_{2p}$ is the mean inverse cube radius for carbon 2p orbitals, and Q_{AB} consists of elements of the charge density and bond order matrix $P_{\mu\nu}$ in the MO theory of the unperturbed molecule¹⁹. The paramagnetic terms involving Q_{AB} arise because the external magnetic field acting on atom B mixes certain excited electronic states of the molecule and thereby induces a current flow on atom A. In the approximation of localized MO wave functions used by Pople, the effect of neighbouring atoms is different from zero only if there is both σ - and π -bonding between atoms A and B, and so it is a multiple bond effect. Q_{AB} depends on orbital hybridization and accordingly $-\sigma_p^{AA}$ is equal to 207 ppm in ethane and 317 ppm in ethylene²⁶.

The local diamagnetic term σ_d^{AA} is given by the Lamb formula (4) and corresponds to a uniform circulation of all atomic electrons as if they were free.

$$\sigma_d^{AA} = \frac{e^2}{3 m c^2} \sum_i \left\langle r_i^{-1} \right\rangle_{av}, \quad (4)$$

where $\left\langle r_i^{-1} \right\rangle_{av}$ is the mean inverse distance of electron from the nucleus A and summation is over electrons on the atom considered. Total variation of this term is much too small to account for the observed range of chemical shifts. With Slater atomic orbitals the variation of σ_d^{AA} for one added 2p or 2s electron is only 14 ppm²⁷ or less than 3 per cent of the total range of observed C¹³ chemical shifts.

The magnetic contributions from bond anisotropy $\sum_{B \neq A} \sigma^{AB}$ are likewise small and do not exceed a few tenths of ppm in most hydrocarbons⁷, except in cyclopropane²⁸. The local paramagnetic term σ_p^{AA} is dominant in determining the chemical shifts of carbon atoms and the variation of this term comes about mostly through the $\left\langle r^{-3} \right\rangle_{2p}$ term

that has a strong charge dependence^{29,27}, although other factors, like variation of ΔE or free-valence index²⁷ may also contribute to a lesser extent. The atomic orbitals of an atom expand with increased negative charge due to interelectronic repulsion and $\left\langle r^{-3} \right\rangle_{2p}$ decreases. Assuming linear dependence of this term on the atomic charge^{27,17}, a linear charge dependence of carbon chemical shift is expected. It has been assumed and found to be consistent with experimental results for a limited class of compounds that gross atomic charges Q_k are analogous to the chemical concept of charge on an atom and should therefore correlate with chemical shifts²⁹.

If the electronic structure of a saturated hydrocarbon could be adequately described with completely localized molecular orbitals, then the variation of Q_{AA} and that of the paramagnetic term should be small^{29,26} and the total variation of chemical shifts of saturated carbon atoms should be less than 14 ppm. Yet the reverse is true. It has been shown^{9,28} that in strained unsaturated molecules a saturated methylene group can have a chemical

shift as low as 117.6 ppm from carbon atoms. A total range of 60 ppm is possible for the groups with sp^3 -hybridised carbon atoms in propane the carbon chemical shift of which is 175.9 ppm⁷. This is a clear indication of delocalization of σ -electrons and in order to get some insight into this phenomenon the resonance spectra of hydrocarbons, with or without strain, were investigated.

Experimental

Low natural abundance makes the registration of carbon-13 spectra quite difficult. The absorption signal is about four orders of magnitude smaller than the corresponding signal from hydrogen of the same molecule. Use of adiabatic rapid passage with a strong measuring rf field

$$\gamma H_1 \gg \frac{1}{H_1} \frac{dH_0}{dt} \gg \frac{1}{T_1}, \frac{1}{T_2},$$

and measuring the dispersion signal has been successful in the study of relatively simple molecules³⁰, but rapid sweep rates and the need for strong measuring rf field γH_1 limit spectral resolution so that the saturated parts of more complex molecules give no useful spectra⁹, Fig. 1. No chemical shifts can be measured from featureless humps and one has either to use exceedingly strong fields and superconducting magnets to generate them or double resonance methods for spectrum simplification. Irradiation of hydrogen atoms near their resonance frequency with a strong perturbing rf field H_2 decouples hydrogen and carbon-13 nuclear spins and to get simple spectra with just one single line for each carbon atom without any visible spin splittings.

If $|\gamma| H_2 \gg |\Delta \omega_2|$; $2\pi |J(C^{13}H)|$, then the residual splitting is^{31,32}:

$$J_r \cong \frac{J \Delta \omega_2}{\gamma H_2},$$

where $|\gamma| H_2$ is the amplitude of the perturbing field and $\Delta \omega_2$ deviation of the perturbing frequency from exact resonance. In our experiments a very strong rf field with an amplitude of 100 cps was used, and since

$$\Delta \omega_2 \ll \pi (\Delta \delta) \cdot 10^6,$$

where $\Delta \delta$ is the full range of hydrogen chemical

does not exceed 1.2 ppm for the saturated terminal alkenes and alkynes³, the residual about 5 cps) is much less than linewidth of the use of a very strong decoupling ν_f of Paul and Grant⁶. No indirect means of the hydrogen resonance frequencies and the perturbing frequency was applied once in each experiment and was optimum decoupling of either all the for unsaturated hydrogen atoms. This work fast and in addition some possible error are avoided⁹.

collapse is accompanied by a correction two- or threefold increase in peak value additional increase in line intensity (and value) is possible as a result of the nuclear effect. Using the symbols of Abrar we have

$$= 1 + (\sigma/\rho) (\Delta\sigma/I_0), \quad (9)$$

ρ is the steady state and I_0 the equilibrium magnetization of the carbon-13 nuclei. $\rho = 1/2$ for dipole-dipole relaxation and $\rho = 1/4$ for an up to threefold increase in intensity is possible. In benzene an increase of up to 5.5 times has been achieved⁹, not always the case since other relaxation interfere, diminishing the σ/ρ ratio.

does not depend on scalar spin-spin and strong enhancement is achieved for saturated sp-carbons in alkynes and carboxylic acids if the methyl and methylene are saturated. For high precision it is to use absorption spectra with a not too disturbing field⁹, but the sensitivity is and the ± 0.07 ppm or even better of little practical use, since unsaturated are susceptible to solvent effects and Because of this adiabatic rapid pass used in most cases and the mean shift both sweep directions calculated. This is simple and allows to work much high sensitivity. The precision is less, 0.5 ppm and relative line intensities are but the mean value for both sweep are unaffected. The spectrometer^{9,38} was 1 apparatus designed to allow all nuclei between 1.5 and 26 Mc to be investigated coupling ν_f power was available only resonance frequency of hydrogen nuclei

(60 Mc). In all cases (monoresonance and spin decoupling, absorption signals and adiabatic rapid passage dispersion signals) time sharing was used with high pulse repetition rate^{39,47}. If the pulse repetition rate is considerably higher than $1/T_2^*$, then all double resonance effects are displayed normally, but base-line stability is greatly improved^{39,47}. The stability of ν_f bridges or crossed coils is not high if very strong decoupling field γH_2 is used and it would be quite difficult to register C¹³ double resonance absorption spectra without the use of pulse methods. The necessary stability of line positions was provided by spin stabilization and a sideband spin generator was used for this purpose. All spectra were registered at 15.1 Mc/sec with a 10 cps/sec frequency sweep and the line positions were measured with an electronic counter. In the case of rapid passage spectra the mean value of measured frequencies for both sweep directions was used. Standard 15 mm test tubes and 1.5 ml of sample (in some cases only 0.25 ml), mostly as neat liquid, were used. All chemical shifts were measured at room temperature from external carbon disulphide, so that

$$\delta_{CS_2} = \sigma_A - \sigma_{CS_2} \quad (10)$$

Results

1. Alkanes.

Normal alkanes up to n-decane and several branched alkanes have been studied by Grant and Paul⁷. Selective spin decoupling was used and all carbon-13 chemical shifts assigned to particular carbon atoms. These assignments are consistent with the constitutive parameters of Savitsky¹². The chemical shifts of saturated methylene groups in n-alkanes cover a range of 16.7 ppm. This, together with quite large vicinal spin-spin coupling constants between hydrogen atoms³⁸, is a clear indication that deviations from perfect pairing, or second order hyperconjugation, does occur in saturated hydrocarbon chains⁹. As a result of this there appear π -bond orders between adjacent saturated carbon atoms^{39,42,43}, $\Delta\sigma$ is no longer zero and gives rise to a paramagnetic shift. In addition to that there appears to be a considerable direct interaction between remote groups, particularly between the end and fourth member of a hydrocarbon chain⁷. Such interactions may play a part in Newman's »rule of six« in chemical reactivity³⁹.

2. Cyclic hydrocarbons.

Only very few investigations have been carried out on these compounds. Savitsky¹² notes, that even simple saturated cyclic structures, such as cyclohexane, show considerable deviations from additivity. In the case of unsaturated cyclic compounds the chemical shifts of only unsaturated sp^2 -carbon atoms have in a few cases been studied¹². We measured the chemical shifts for a small representative series of cyclic compounds that allowed us to investigate the effect of strain and unsaturation on carbon chemical shifts^{3,28}. The results are listed in table 1.

It is apparent that chemical shifts of saturated carbon atoms in saturated cyclic compounds are not very susceptible to strain. The carbon-13 chemical shifts of adamantane, that is completely free of strain and rigid are very similar to the chemical shifts of strained norbornane (strain energy, 18.5 kcal mole⁴⁰), and if one uses the +6 ppm correction for every saturated 5- or 6-membered ring, then these shifts are quite comparable with chemical shifts of carbon atoms in normal and branched alkanes. However, quite unusual chemical shifts occur in unsaturated strained polycyclic compounds. The bridge methylene carbon

Table 1: Chemical shifts δ_{CS_2} of some cyclic hydrocarbons.

Molecule	Carbon atom	Exptl. ^a $\delta_{CS_2}^a$	Calcd. ^b $\delta_{CS_2}^b$	Δ $\delta_{CS_2}^a - \delta_{CS_2}^b$	Calcd. ^c $\delta_{CS_2}^c$
Adamantane	CH ₂ CH	155.5 165.0	147.2 145.5	+ 8.3 + 19.5	159.2 163.5
Norbornane	CH ₂ (7) CH (1, 4) CH ₂ (2, 3, 5, 6)	155.0 157.5 163.0	147.2 145.4 154.1	+ 7.8 + 12.1 + 8.9	159.2 157.4 166.1
Norbornene ^d	CH ₂ (7) CH (1, 4) CH ₂ (5, 6) = CH (2, 3)	140 148 160 56	147.2 146.1 154.1 56.2	— 7.2 + 1.9 + 5.9 — 0.2	— 146.1 154.1 56.2
Norbornadiene	CH ₂ (7) CH (1, 4) = CH (2, 3, 5, 6)	117.6 142.5 49.5	147.2 146.8 56.2	— 29.6 — 4.3 — 6.7	— 146.8 56.2
Quadracyclene ^e	CH (1, 4) CH (2, 3, 5, 6)	171.0 179.0	131.6 124.7	+ 39.4 + 54.3	—

^a) ± 1 ppm.

^b) Calculated on the basis of constitutive bond parameters³⁵.

^c) Calculated on the basis of constitutive bond parameters with a diamagnetic constitutive +6 ppm for every independent 5- or 6-membered saturated ring structure connected with atom under consideration. Adamantane is considered to contain 3 rings for every CH₂ group.

^d) For every CH₂ group.

^e) Sample was partially decomposed and impure, chemical shift of carbon-7 could not be acceptable accuracy.

in both norbornene and norbornane large paramagnetic shift, as compared to adamantane. Clearly, two different mechanisms operative in determining the methyl shifts in cyclic compounds. If one takes usual assumption of perfect pairing of π -bonds, then one has two kinds of for the σ -electrons. Both act in the same way and lead to a paramagnetic shift. One hydrocarbons and is not particularly to strain while the other needs π nearby atoms and is met only in unsaturated cyclic compounds. In such molecules with strain. In such molecules with strain⁴¹, a strong hyperconjugative interaction⁴² between π -electrons and the bridge carbons possible and the resulting bondings are classical. The electron structure of carbon atom may no longer be adequately by sp^3 -hybrids, this makes σ^{AA} large to a paramagnetic shift.

Since both these mechanisms can significant paramagnetic terms that contribute a strong general charge dependent chemical shifts is expected. Any decoupling charge must lead to paramagnetic

methylene and methine carbons in norbornadiene can be compared with the chemical shifts of α -alkenes and even alkanes (see Table 1). Clearly, rigid molecules with high strain and a special geometric arrangement between the interacting groups are necessary for the special, norbornadiene kind of hyperconjugation to take place.

4. Alkynes.

Carbon-13 spectra of a few simple acetylenes have been studied by Lauterbur⁴⁶, Friedel and Retcofsky⁴⁷, and others^{47,48}. Only the chemical shifts of the sp-hybridized carbon atoms were measured and found to fall into the rather narrow range 104 to 126 ppm from CS₂^{49,50} that is usually free from other carbon-13 signals and can be used for the identification of triple bonds. Very little is known about the chemical shifts of saturated carbon atoms in alkynes. Methyl and methylene groups of these molecules give very complicated spectra of weak overlapping multiplets where no determination of chemical shifts is possible. We investigated some representative alkynes¹⁰ and complete chemical shift data for these normal alkynes together with the calculated values are given in the Table 3. The values for n-octane⁷ are added for comparison. The assignment of the chemical shift to a given carbon atom was made on the basis of peak intensities, additive parameters and in some cases through the use of monoresonance spectra and selective decoupling with various $\Delta\nu_2$ values.

The data for the alkynes indicate that quite regular trends exist for the chemical shift values. The chemical shifts of carbon atoms in the higher members conform very well with trends established by earlier members of the series where there is no ambiguity in spectral assignment. It is immediately apparent that the triple bond influences only the shifts of immediate neighbours, the α -carbon atoms, that show a fairly constant diamagnetic shift about 11 to 13 ppm for both methyl and methylene groups. The possible effect on β -carbon atoms is certainly less than 1 ppm if it exists at all and the shifts of β,γ and farther atoms correspond closely to the shifts in similar alkanes. The diamagnetic 11 ppm shift of α -methylene carbon atoms relative to atoms in the same position in paraffins is large. As a result of this shift, in some cases the α -methylene groups absorb in a higher field than the methyl groups of the same molecule. If this shift is caused by magnetic anisotropy of the triple bond, then this anisotropy must be even

Table 3: Carbon-13 chemical shift data for unbranched alkynes.

Carbon atom	Hexyne-1	Hexyne-2	Hexyne-3	Heptyne-1	Heptyne-2	Heptyne-3	Octyne-1	Octyne-2	Octyne-3	Octyne-4
C ₁	Exptl. ¹ Calcd. ² Δ^3	125.1 125.8 -0.7	190.8 189.4 +1.4	178.1 176.6 +1.5	125.1 125.8 -0.7	190.2 189.4 +0.8	178.8 176.6 +2.2	123.5 125.8 -2.3	189.6 189.4 +0.2	177.4 176.6 +0.8
C ₂	Exptl. Calcd. Δ	109.7 110.2 -0.5	118.8 118.7 +0.1	180.5 182.3 -1.8	109.6 110.2 -0.6	118.3 118.7 -0.4	180.5 182.3 -1.8	108.5 110.2 -1.7	117.7 118.7 -1.0	179.5 182.3 -2.8
C ₃	Exptl. Calcd. Δ	175.1 173.8 +1.3	115.6 110.2 +5.4	112.6 110.2 +2.4	174.8 173.8 +1.0	114.9 110.2 +4.7	114.2 110.2 +4.0	174.1 173.8 +0.3	114.0 110.2 +3.8	112.8 110.2 +2.6
C ₄	Exptl. Calcd. Δ	162.6 161.0 +1.6	172.9 173.8 -0.9	112.6 110.2 +2.4	164.4 161.0 +3.4	174.8 173.8 +1.0	112.3 110.2 +2.1	163.3 161.0 +2.3	174.1 173.8 +0.3	111.5 110.2 +1.3
C ₅	Exptl. Calcd. Δ	171.3 169.5 +1.8	170.9 169.5 +1.4	180.5 182.3 -1.7	161.8 161.0 +0.8	161.3 161.0 +0.3	172.3 173.8 -1.5	163.3 161.0 +2.3	163.0 161.0 +2.0	173.8 173.8 0.0
C ₆	Exptl. Calcd. Δ	179.6 176.6 +3.0	180.4 176.6 +3.8	178.1 176.6 +1.5	170.1 169.5 +0.6	170.7 169.5 +1.2	170.0 169.5 +0.5	160.5 161.0 -0.5	161.1 161.0 +0.1	160.6 161.0 -0.4
C ₇	Exptl. Calcd. Δ				178.5 176.6 +1.9	179.0 176.6 +2.4	179.4 176.6 +2.8	169.1 169.5 -0.4	169.8 169.5 +0.3	169.7 169.5 +0.2
C ₈	Exptl. Calcd. Δ							177.6 176.6 +1.0	178.0 176.6 +1.4	177.9 176.6 +1.3

¹ ppm from external CS₂, without corrections for bulk susceptibility, $\delta_{C_4H_6} - \delta_{CS_2} = 65$ ppm.

² Calculated with the use of the constitutive parameters of G. B. Savitsky¹².

³ Δ stands for the difference $\delta_{\text{exptl.}} - \delta_{\text{calcd.}}$.

⁴ D. M. Grant and E. G. Paul⁷.

larger than the highest suggested value⁵¹. The difference of chemical shifts of the two sp-carbon atoms has analytical value. It is 15.2 ± 0.3 ppm in 1-alkynes, 3.4 ± 0.3 ppm in 2-alkynes and 1.6 ± 0.3 ppm in 3-alkynes. These values have significance for higher members of the series only, in the case of butynes and phenylacetylene there are large deviations from these values¹⁷.

The differences between calculated¹² and measured chemical shifts are small and show that the Savitsky parameters can well be used in the structural analysis of aliphatics. One new constant for the $-C \equiv C-$ group, +29 ppm has been added. The equality to the $\equiv C-$ constant must be purely accidental.

The Overhauser effects provide some insight into the relaxation processes in alkynes. A large increase of line intensity of unsubstituted sp-carbon atoms was noted, even though only more distant hydrogen atoms were saturated. This is consistent with the relative insignificance of other relaxation mechanisms for these spins⁴⁶, but a very small Overhauser effect on the α -methyl groups has been observed.

since no very effective additional relaxation mechanisms for sp³-carbon atoms are known.

5. Alkenes

Carbon-13 spectra of unsaturated compounds have been actively investigated. The results of H. J. Cantow and R. E. Marchessault⁵² showed that olefinic carbon nuclei absorb in the same region as aromatic carbons. In the absence of polar substituents the absorption falls into a very crowded region of 44 to 79 ppm from Substituents cause additional shifts and the range reaches from 38 to 114⁵⁰. A systematic shift of unsaturated carbon atoms of olefins has been reported by Friedel and Retcofsky⁴¹ and by Lauterbur⁴⁶. These results, it has been shown that simple hydrocarbons the chemical shift of unsaturated sp²-carbon atoms is a constant property that depends on the nearest neighbor only⁵². The saturated chains of alkenes received little attention. We investigated all metric isomers of normal octenes⁵¹ where in cases it was possible to separate eight distinct

Exptl.	Molecule	Exptl.
1.2	1,4-Pentadiene ⁴¹	154
1.5	1,5-Hexadiene ⁴¹	158
1.7	Diphenylmethane ⁴¹	157
1.9	Dibenzyl	154.9

Table 2: Chemical shifts δ_{CS_2} of methylene groups in norbornadiene compounds.

1. L. Retcofsky⁴¹,
D. M. Grant, E. B. Baker, G. A.

s that does not exceed 1.2 ppm for the saturated carbons of normal alkenes and alkynes⁹, the residual coupling (about 5 cps) is much less than linewidth $\Delta\nu$. The use of a very strong decoupling ν_f is the main difference of our technique from the method of Paul and Grant⁶. No indirect measurement of the hydrogen resonance frequencies was attempted and the perturbing frequency was changed only once in each experiment and was tested for optimum decoupling of either all the saturated or unsaturated hydrogen atoms. This is not to work fast and in addition some possibilities of error are avoided¹⁹.

$$\langle I_z \rangle = 1 + (\sigma/\rho) (\mathcal{S}_0/I_0), \quad (9)$$

where $\langle I_z \rangle$ is the steady state and I_0 the equilibrium magnetization of the carbon-13 nuclei. The $\sigma/\rho = 1/2$ for dipole-dipole relaxation and $\sigma/\rho = \gamma_H/\gamma_C \cong 4$ an up to threefold increase in intensity is possible. In benzene an increase of σ value up to 5.5 times has been achieved⁹, this is not always the case since other relaxation processes²⁵ interfere, diminishing the σ/ρ ratio.

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^c Calculated on the basis of constitutive bond parameters with a diamagnetic contribution +6 ppm for every independent 5- or 6-membered saturated ring structure common atom under consideration. Adamantane is considered to contain 3 rings for every CH₂ group.

^d From earlier work¹⁷.

^e Sample was partially decomposed and impure, chemical shift of carbon-7 could not be acceptable accuracy.

in both norbornene and norbornane. Clearly, two different operative in determining the shifts in cyclic compounds. The usual assumption of perfect π -bonds, then one has two kinds for the σ -electrons. Both act in and lead to a paramagnetic shift of hydrocarbons and is not parallel to strain while the other one nearby atoms and is met only with strain. In such molecules^{22,41} a strong hyperconjugation between π -electrons and the σ -electrons and the resulting bond classical. The electron structure of carbon atom may no longer be by sp^3 -hybrids, this makes σ_{CH} to a paramagnetic shift.

Since both these mechanisms significant paramagnetic terms a strong general charge delocalization chemical shifts is expected. An charge must lead to paramagnetic terms.

theory with a basis set consisting of a 1s Slater orbital on each hydrogen atom in the molecule, and 2s and 2p Slater orbitals on each carbon atom. All neighbour and non-neighbour interactions are included (non-zero differential overlap) and the complete secular determinant is treated. A somewhat different approach has been used by Whitehead. His self-consistent group orbital and bond electronegativity (SGOBE) method^{23,24} and the extended Hückel theory (EHT) have both been used for charge calculations and gross atomic charge Q_k has been found to correlate successfully with the carbon chemical shifts²³, thereby providing an important link between theoretical calculations and experiment.

The total screening of a nucleus can be divided into a diamagnetic and a paramagnetic contribution from local currents associated with the given atom A, contributions from local currents on other atoms B and effects of molecular ring currents that cannot be localized^{25,26}. The magnetic field at nucleus A is

$$H_A = H_o (1 - \sigma^A), \quad (1)$$

where σ^A is the total shielding constant of a particular nucleus.

$$\sigma^A = \sigma_p^{AA} + \sigma_d^{AA} + \sum_{B \neq A} \sigma^{AB} + \sigma^{A, \text{ring}} \quad (2)$$

The local paramagnetic term is given by

$$\sigma_p^{AA} = -\frac{e^2 b}{2m^2 c^2 \Delta E} \left\langle r^{-3} \right\rangle_{2p} \sum_B Q_{AB}, \quad (3)$$

where ΔE is the mean $\sigma \leftrightarrow \pi$ excitation energy, usually 5 to 10 eV, $\left\langle r^{-3} \right\rangle^{2p}$ is the mean inverse cube radius for carbon 2p orbitals, and Q_{AB} consists of elements of the charge density and bond-order matrix $P_{\mu\nu}$ in the MO theory of the unperturbed molecule¹⁹. The paramagnetic terms involving Q_{AB} arise because the external magnetic field acting on atom B mixes certain excited electronic states of the molecule and thereby induces a current flow on atom A. In the approximation of localized MO wave functions used by Pople, the effect of neighbouring atoms is different from zero only if there is both σ - and π -bonding between atoms A and B, and so it is a multiple bond effect. Q_{AB} depends on orbital hybridization and accordingly $-\sigma_P^{AA}$ is equal to 207 ppm in ethane and 317 ppm in ethylene²⁰.

The local diamagnetic term $\sigma_d^{\Lambda\Lambda}$ is given by the Lamb formula (4) and corresponds to a uniform circulation of all atomic electrons as if they were free.

$$\sigma_{\text{d}}^{\text{AA}} = \frac{e^2}{3mc^2} \sum_i \langle r_i^{-1} \rangle_{\text{av}}, \quad (4)$$

where $\langle r_i^{-1} \rangle_{av}$ is the mean inverse distance of electron from the nucleus A and summation is over electrons on the atom considered. Total variation of this term is much too small to account for the observed range of chemical shifts. With Slater atomic orbitals the variation of σ_d^{AA} for one added 2p or 2s electron is only 14 ppm³⁷ or less than 3 per cent of the total range of observed C^{13} chemical shifts.

The magnetic contributions from bond anisotropy $\sum_{B \neq A} \sigma^{AB}$ are likewise small and do not exceed a few tenths of ppm in most hydrocarbons⁷, except in cyclopropane²⁹. The local paramagnetic term σ_p^{AA} is dominant in determining the chemical shifts of carbon atoms and the variation of this term comes about mostly through the $\langle r^{-3} \rangle$ term

that has a strong charge dependence^{26,27}, although other factors, like variation of ΔE or free-valence index²⁷ may also contribute to a lesser extent. The atomic orbitals of an atom expand with increased negative charge due to interelectronic repulsion and $\langle r^{-3} \rangle_{sp}$ decreases. Assuming linear dependence of this term on the atomic charge^{27,17}, a linear charge dependence of carbon chemical shift is expected. It has been assumed and found to be consistent with experimental results for a limited class of compounds that gross atomic charges Q_K are analogous to the chemical concept of charge on an atom and should therefore correlate with chemical shifts²⁹.

If the electronic structure of a saturated hydrocarbon could be adequately described with completely localized molecular orbitals, then the variation of Q_{AA} and that of the paramagnetic term should be small^{25,26} and the total variation of chemical shifts of saturated carbon atoms should be less than 14 ppm. Yet the reverse is true. It has been shown^{9,28} that in strained unsaturated molecules a saturated methylene group can have a chemical

shift as low as 117.6 ppm from carbon atoms. A total range of 60 ppm is possible for groups with sp^3 -hybridised carbon atoms in propane the carbon chemical shift is 175.9 ppm⁷. This is a clear indication of delocalization of σ -electrons and in order to get some insight into this phenomenon the resonance spectra of hydrocarbons, without strain, were investigated.

Experimental

Low natural abundance makes the region of the carbon-13 spectra quite difficult. The signal is about four orders of magnitude below the corresponding signal from hydrogen in the same molecule. Use of adiabatic rapid passage with a strong measuring *rf* field

$$1 - \frac{dH_0}{dH_1} \geq \frac{1}{T_1} \wedge \frac{1}{T_2},$$

and measuring the dispersion signal is successful in the study of relatively simple molecules²⁰, but rapid sweep rates and the strong measuring ν_f field γH_f limit spectrum resolution so that the saturated parts of more complex molecules give no useful spectra⁹, Fig. 1. No chemical shifts can be measured from featureless humps and one has either exceedingly strong fields and superconducting magnets to generate them or double resonance methods for spectrum simplification. Irradiation of hydrogen atoms near their resonance frequency with a strong perturbing ν_f field H_s decouples the hydrogen and carbon-13 nuclear spins and so get simple spectra with just one singlet for each carbon atom without any visible splittings.

if $|\gamma| H_2 > |\Delta \omega_2|$; $2\pi |J(C^{13}\text{H})|$, then the residual splitting is^{32,33}:

$$I_r \equiv \frac{J \Delta \omega_2}{\gamma H_2},$$

where $|\gamma|/H_a$ is the amplitude of the perturbation field and $\Delta\omega_2$ deviation of the perturbation frequency from exact resonance. In our experiment a very strong rf field with an amplitude of 100 gauss was used, and since

$$\Delta\omega_2 < \pi(\Delta\delta) \cdot 10^6,$$

where $\Delta\delta$ is the full range of hydrogen

complete chemical shift data for the alkenes as well as the calculated values¹² and the deviations given in the Table 4. The assignment of carbon chemical shifts to particular carbon atoms was made on the basis of regular deviations from the corresponding values in similar unsaturated or saturated compounds (n-octane), additive parameters^{7,12}, peak intensities and through the use of selective decoupling with various $\Delta\omega_2$ values. The chemical shift data indicate that both the α - and β -carbon shifts fall into the corresponding usual ranges⁵⁰. In the case of asymmetrically substituted double bonds in linear molecules the difference of chemical shifts of the unsaturated carbon atoms has analytical significance. It is 24 ppm in octene-1, 7 ppm in octene-2 and 1.6 ppm in octene-3. There is every reason to expect similar differences in higher alkenes. These differences are practically identical in both cis and trans isomers. The chemical shifts of saturated carbon atoms are such that the double bond influences the shielding of immediate neighbours only and there is no inductive effect on β or γ -carbon atoms. The shifts of these and other carbon atoms are very close to

Table 4: Carbon-13 chemical shift data for normal alkenes.

Carbon atoms	Octene-1	cis-Octene-2	trans-Octene-2	cis-Octene-3	trans-Octene-3	cis-Octene-4	trans-Octene-4	n-Octane ⁴
Exptl. ¹ Calcd. ² Δ^3	78.7 78.7 0.0	180.7 177.3 +3.4	174.7 177.3 -2.6	179.0 176.6 +2.4	179.2 176.6 +2.6	179.4 176.6 +2.8	178.8 176.6 +2.2	179.7 176.6 +3.1
Exptl. Calcd. Δ	54.5 55.9 -1.4	70.0 71.6 -1.6	68.5 71.6 -3.1	173.0 170.2 +2.8	168.3 170.2 -1.9	170.5 169.5 +1.0	169.6 169.5 +0.1	170.7 169.5 +1.2
Exptl. Calcd. Δ	158.7 161.7 -3.0	62.8 63.1 -0.3	61.2 63.1 -1.9	64.4 63.1 +1.3	63.5 63.1 +0.4	164.3 161.7 +2.6	158.0 161.7 -3.7	161.3 161.0 +0.3
Exptl. Calcd. Δ	162.6 161.0 +1.6	167.0 161.7 +5.3	160.2 161.7 -1.5	63.2 63.1 -0.1	61.5 63.1 -1.6	64.4 63.1 +1.3	62.3 63.1 -0.8	164.0 161.0 +3.0
Exptl. Calcd. Δ	162.6 161.0 +1.6	163.9 161.0 +2.9	162.4 161.0 +1.4	166.9 161.7 +5.2	161.5 161.7 -0.2	64.4 63.1 +1.3	62.3 63.1 -0.8	164.0 161.0 +3.0
Exptl. Calcd. Δ	159.9 161.0 -1.1	161.8 161.0 +0.8	160.2 161.0 -0.8	161.5 161.0 +0.5	161.5 161.0 +0.5	164.3 161.7 +2.6	158.0 161.7 -3.7	161.3 161.0 +0.3
Exptl. Calcd. Δ	169.4 169.5 -0.1	170.4 169.5 +0.9	169.5 169.5 0.0	171.0 169.5 +1.5	170.9 169.5 +1.4	170.5 169.5 +1.0	169.6 169.5 +0.1	170.7 169.5 +1.2
Exptl. Calcd. Δ	178.3 176.6 +1.7	179.1 176.6 +2.5	178.2 176.6 +1.6	179.0 176.6 +2.4	179.2 176.6 +2.6	179.4 176.6 +2.8	178.8 176.6 +2.2	179.7 176.6 +3.1

from CS₂, without corrections for bulk susceptibility, $\delta_{\text{Calc}} - \delta_{\text{CS}_2} = 65$ ppm. The assignments of carbon chemical shifts to particular carbon atoms were made on the basis of regular deviations from the corresponding values in similar unsaturated or saturated compounds (n-octane), additive parameters^{7,12}, peak intensities and through the use of selective decoupling with various $\Delta\omega_2$ values. The chemical shift data indicate that both the α - and β -carbon shifts fall into the corresponding usual ranges⁵⁰. In the case of asymmetrically substituted double bonds in linear molecules the difference of chemical shifts of the unsaturated carbon atoms has analytical significance. It is 24 ppm in octene-1, 7 ppm in octene-2 and 1.6 ppm in octene-3. There is every reason to expect similar differences in higher alkenes. These differences are practically identical in both cis and trans isomers. The chemical shifts of saturated carbon atoms are such that the double bond influences the shielding of immediate neighbours only and there is no inductive effect on β or γ -carbon atoms. The shifts of these and other carbon atoms are very close to

symmetrically placed sp^3 -carbon atoms. Magnetic effects must be very small in unsubstituted normal alkenes, since the ~ 0.05 ppm differences of olefinic, α -methyl and α -methylene proton shifts in cis- and trans isomers are nearly two orders of magnitude smaller than in carbon spectra, with opposite signs for α -methyl and α -methylene protons². Steric inhibition of conjugation, as suggested for bulky substituents⁵⁵ is quite improbable for the flexible alkyl groups where only hyperconjugation is possible, but some other forms of action through space^{5,56} cannot be entirely discounted. However, since all atoms of the molecule are affected a systematic difference in ΔE suggests itself. The only strong ultraviolet absorption band of normal alkenes is for cis-2-alkenes $\lambda_{\text{max}}^{\text{cis}} = 176.5 \pm 1.5 \text{ m}\mu$ and for trans-2-alkenes $\lambda_{\text{max}}^{\text{trans}} = 179 \pm 1 \text{ m}\mu$ ⁵⁷. If the paramagnetic contribution to the chemical shift σ_p^{AA} has in alkenes about the same values as in ethylene⁵⁶, then a 1.8 ppm/m μ change in chemical shift values is to be expected and gives the right order of magnitude for the shift differences, although most of these are actually smaller. An analogous analysis of chemical shifts in cyclic ketones gave very similar results where the actual effect was likewise only about half of the predicted value⁵⁸.

With the exception of α -carbon atoms all calculated shifts¹² agree well with the measured values. The Savitsky parameters can be used to predict the spectra of normal alkenes and the chemical shifts of α -carbon atoms allow the geometric isomers to be recognized.

Table 5: Carbon-13 chemical shift data for carboxylic acids.

Molecule	Chemical shifts of carbon atoms						
	C ₁	C ₂	C ₃	C ₄	C ₅	C ₆	C ₇
Formic acid ^a	27.0	174.2					
Acetic acid ^a	15.6	174.2					
Propionic acid	12.1	166.1	184.0				
n-Butyric acid	12.5	157.1	174.6	179.1			
n-Valeric acid	12.5	159.1	165.8	170.2	179.3		
n-Caproic acid	12.7	159.2	168.5	161.1	170.0	178.9	
n-Enanthic acid	12.6	158.6	167.7	163.2	160.0	169.5	178.3
Oxalic acid	32.8	32.8					
Malonic acid	23.3	152.3	23.3				
Succinic acid	17.3	163.7	163.7	17.3			
Glutaric acid	16.6	160.0	171.7	160.0	16.6		
Adipic acid	16.4	159.0	168.0	168.0	159.0	16.4	
Pimelic acid	16.0	158.3	167.5	163.6	163.6	167.6	16.0
Suberic acid	16.2	158.8	167.6	163.7	163.7	167.9	15.8
Azelic acid	16.0	159.2	167.9	163.2	163.2	163.2	16.2
Sebacic acid	16.2	158.8	167.8				
Propaneh ^b	176.3	175.9	176.3				
n-Pentane ^b	180.0	171.1	159.2	171.1	180.0		
n-Decane ^b	179.6	170.7	161.3	163.8	163.4	163.4	163.8

^a J. B. Brothers, P. C. Lauterbur⁶⁰.

^b Data for the difference $\delta_{\text{expt}} - \delta_{\text{calcd}}$.

